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A NONLINEAR-PHASE, MODEL-BASED HUMAN DETECTOR FOR RADAR (PREPRINT)

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A Nonlinear-Phase, Model-Based Human Detector for Radar

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Abstract—**Radar offers unique advantages over other sensors for the detection of humans, such as remote operation during virtually all weather and lighting conditions. Many current radar-based human detection systems employ some type of Fourier analysis, such as spectrograms. However, in many environments, the signal-to-noise ratio (SNR) for human targets is quite low and the spectrogram is almost completely masked by clutter. Furthermore, Fourier-based techniques assume a linear target phase, whereas human targets have a highly nonlinear phase history. The resulting phase mismatch causes significant SNR loss in the detector itself. In this paper, human modeling is used to derive a more accurate non-linear approximation to the true target phase history. The likelihood ratio is optimized over unknown model parameters to enhance detection performance. Cramer-Rao bounds (CRB) on parameter estimates and receiver operating characteristic (ROC) curves are used to validate analytically the performance of the proposed method and to evaluate simulation results.**

Index Terms—**Human detection, radar signal processing, synthetic aperture radar, detection and estimation.**

I. INTRODUCTION

O VER the last decade a variety of Fourier-based techniques have been applied to detect human targets in differing situations using radar. For example, Yarovoy [1] used ultra-wide band (UWB) radar to locate humans trapped in buildings by sensing respiratory motions. The radar returns from breathing and non-breathing targets were separated by analyzing the spectral variations of the radar return. Falconer [2] utilized differences in the shape of the power spectral density (PSD) of the return signal from a pulsed-Doppler microwave radar placed outside a building to differentiate between targets and infer the activity level of humans inside, discerning only large movements. Sabatini [3] applied wavelet analysis to the time varying-range profile measured with sonar

to find human targets. All of these aforementioned techniques attempt to pick out probable human targets by identifying low-frequency periodic motion, which can be confused with the motion of other non-human targets, such as a slowly spinning ceiling fan.

The first attempts at developing detection algorithms that focused on features unique to human targets began with work by Weir [4] in 1997, where he developed the concept of a "gait velocitygram" – the velocity profile of a human target as seen by a sonar, or ultrasonic ranging device. The velocitygram contained distinct features that were used to calculate gait parameters, such as walking speed, cadence, step length, step time, and time to steady state walking. Indeed, work on gait analysis using visual and seismic sensors has led researchers to suggest that the human gait may become a biometric parameter that could be used for identification, just like fingerprints or hand geometry [5].

Frequency-based concepts were refined with the concept of the "radar gait signature" – a spectral analysis of the gait signature that has been shown to be characteristic of humans [5,6,7,8,10]. Although Geisheimer [6] initially used chirplet transforms to characterize the gait signature, spectrograms have been proposed as a simpler way of extracting biomechanical information from the radar return. In 2002, Geisheimer [7] experimentally verified that the overall spectrogram from a human target matched the sum of spectrograms constructed from the returns of individual body parts. The theoretical basis for this result was developed by Van Dorp [8], who divided the human body into 12 parts and computed the time-varying range for each part using a walking model developed by Thalmann [9]. Van Dorp showed that the human model-based simulated gait signatures matched the spectrograms derived from measured data – an important result that will serve as the basis for the human model utilized in this paper.

This foundation has led to much work that exploits the unique features of the human spectrogram. For example, Otero [10] used the spectrogram to compute features such as the stride and appendage/torso ratio. Plotting the velocity and appendage/torso ratio for pedestrians passing by, Otero observed that male and female targets were roughly grouped in different regions on the grid, suggesting that such features may be used for gender discrimination. As another example, Greneker [11] exploited the changes in stride and velocity caused by the weight of a load around the waist to propose a

spectrogram-based suicide bomber detection system.

These techniques aim at applying spectrograms to characterize targets already detected through Doppler or Fourier-based processing and were used in close proximity to the target or in situations where interference was minimal. In practice, spectrograms are often completely obscured in high clutter environments, rending impossible the accurate estimation of any feature or parameter that is to be used to discriminate humans from other targets [12]. Moreover, since human targets have relatively weak returns in comparison to vehicles or other objects, detecting even the existence of a human target is more difficult. In the event that a detector fails to detect a probable human target, any of the above characterization techniques cannot be applied.

Note that the Fourier transform implements a linear-phase filter yielding a peak response only when the target phase is also linear. In fact, the phase history for human targets is non-linear [13], so that the resulting phase mismatch causes a significant loss in output signal-to-noise ratio (SNR) inherent to the detector as the dwell increases, thereby degrading detection performance.

The goal of this paper is to derive a new, nonlinear-phase detector such that the phase mismatch between detector and target phase is minimized, and thus output SNR and probability of detection are maximized. In Section II, Thalmann's kinematic model for human walking is used as a basis for deriving an analytic expression of the true human target phase and for generating the synthetic human radar data used in our computer simulations. The deficiency of linear phase detectors is evaluated in Section III, which introduces spectrograms and analyzes the output signal-to-noise ratio (SNR) losses of Fourier-based methods. In Section IV, the proposed human model-based optimized nonlinear phase (ONLP) detector is derived. Maximum likelihood estimates (MLE) of unknown geometry and model parameters are obtained to maximize the likelihood ratio and resulting matched filter output. Cramer-Rao bounds of parameter estimates are used to illustrate the impact of modeling error on performance. Finally, in Section V, the detection performance of FFT-based matched filters is compared to that of the proposed ONLP detector, as well as to the ideal "clairvoyant" detector, representing the best performance attainable with complete knowledge of target parameters.

II. SIGNAL MODELING

A. Received Signal

In general, the received radar signal is a time-delayed, frequency-shifted version of the transmitted chirp signal. Then the return for a point target may be expressed as

$$s_r(n,t) = a_t rect\left(\frac{\hat{t} - t_d}{\tau}\right) e^{j[-2\pi f_c t_d + \pi\gamma(\hat{t} - t_d)]}, \quad (1)$$

where the time t is defined as $t = T(n-1) + \hat{t}$ in terms of the

pulse repetition interval (PRI), T, the pulse number, n, and the time relative to the start of each PRI, $\hat{t}$; a_t is the amplitude as given by the radar range equation; τ is the pulse width; c is the speed of light; γ is the chirp slope; f_c is the transmitted center frequency; and t_d is the round trip time delay between antenna and target, defined in terms of the target range, R, as $t_d = 2R/c$.

Exploiting the work of Geisheimer and Van Dorp, who showed that a human target could be divided into parts and the total response obtained by simply summing the responses of each part – i.e., that the principle of superposition could be applied to human modeling – the radar return from a human target may be mathematically expressed as

$$s_h(n,t) = \sum_{i=1}^{K} a_{t,i} rect\left(\frac{\hat{t} - t_{d,i}}{\tau}\right) e^{j[-2\pi f_c t_{d,i} + \pi\gamma(\hat{t} - t_{d,i})]}, \quad (2)$$

where K are the number of point targets comprising the overall human target.

The amplitude $a_{t,i}$, defined as

$$a_{t,i} = \frac{G\lambda\sqrt{P_t \sigma_i}\,\sigma_n}{(4\pi)^{1.5} R_i^2 \sqrt{L_s}\sqrt{L_a}\sqrt{T_{sys}}}, \quad (3)$$

includes several factors which vary with target range, R_i, and geometry. For instance, the antenna gain, G, varies according to angle of incidence, and the atmosphere losses, L_a, vary with range. For simplicity, we assume that these parameters are constant, along with the transmitted signal power, P_t, the wavelength, λ, the system loss, L_s, the system temperature, T_{sys}, and the noise standard deviation, σ_n. The radar cross section (RCS), σ_i, is modeled according to the shapes of the body parts. Thus, the head is modeled as a sphere and the other body parts as cylinders.

B. Human Model

A human is a complicated target because of the intricate motion of body parts moving along different trajectories at different speeds. In this work, the human body is divided into twelve basic body parts: the head, upper arms, lower arms, torso, thighs, lower legs and feet. As indicated in Fig. 1, each point target is taken to lie at the center of the corresponding body part.

The time-varying position of each point target may be computed using the kinematic model of a walking human developed by Thalmann [9]. In the Thalmann model, all positions are referenced to the base of the spine, denoted by
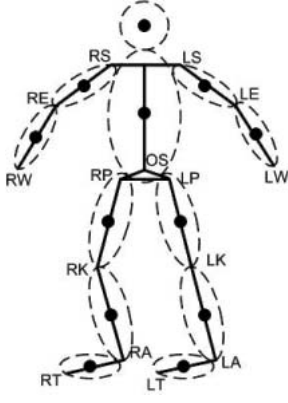
Figure 1. 12-point human model [12].

OS. Over the course of one cycle (two steps), the vertical, lateral, and translational position of OS varies sinusoidally. The time-varying angles of the joints are also provided by means of charts and equations in [9]. Together with the dimensions of the human body, these time-varying joint angles may be used to compute the time-varying positions of each point target relative to OS and each of the time delays ($t_{d,i}$) required in (2).

C. Data Generation

To test and evaluate the proposed algorithms, the radar signal and human model equations described above are used to generate simulated radar data in MATLAB. The slow-time, fast-time data matrix is pulse compressed so that the peak occurs at the range bin in which the target is present. Taking a slice across slow-time at the range bin of the peak output,

$$x_p[n] = \sum_{i=1}^{12} a_{t,i}\tau e^{-j\frac{4\pi f_c}{c}R_{d,i}} \ , \qquad (4)$$

where $R_{d,i}$ is the range from the antenna to the center of each body part.

Spectrogram-based algorithms as well as the new method proposed in this paper use the slow-time slice in (4) as the starting point for data processing.

III. HUMAN SPECTROGRAMS

A. Computation

The spectrogram of a human target may be computed by stacking the fast Fourier transforms (FFT) of short, overlapping time segments taken from the slow-time slice in (4). An example of the simulated spectrogram for a human target is shown in Fig. 2.

The strongest return is received from the torso, with its low-frequency, small-amplitude sinusoidal oscillatory motion. The appendages that travel the farthest during the walking cycle – the feet – appear in the spectrogram with the largest amplitude oscillation. Note that the special nature of the

periodicities within the human spectrogram are what makes this response unique and differentiable from the spectrograms of even other animals, as can be seen from the measured spectrograms of a human and dog given by Otero in [10]. The human spectrogram measured by Otero also compares well with the spectrograms generated based on our human model.

In many practical environments, however, the impact of clutter and noise is significant in masking human targets, which are weak in comparison to other objects with higher RCS, such as automobiles. When the pulse-wise SNR drops to -15dB, even the torso return is difficult to discern (Fig. 3). Thus, for many practical radar problems, the spectrogram is of little help in discriminating human targets from other objects.
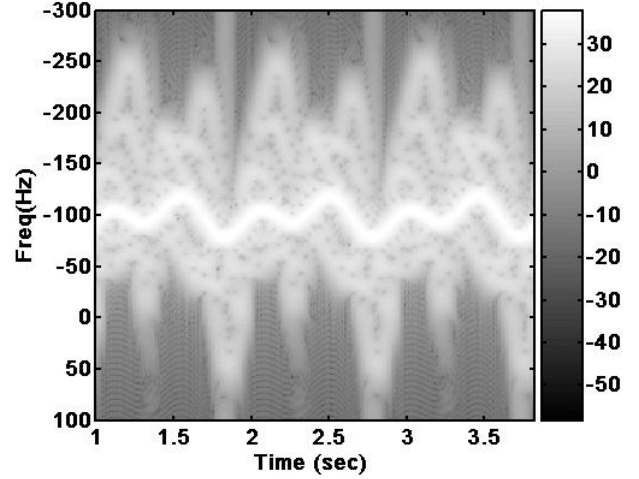

Figure 2. Simulated human spectrogram.

Figure 3. Human spectrogram in noise with SNR = -15dB.

B. Inherent SNR loss in Fourier-based detectors

More importantly, the Fourier transforms used in calculating the spectrogram or in Doppler processing are inherently linear phase matched filters. However, the phase history of a human target can be highly nonlinear, resulting in an inherent SNR loss when matched filtered with a linear-phase filter, such as the FFT. Consider the phase history of a typical human target

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walking at a 45° incidence angle relative to the initial antenna-target vector, as shown in Fig. 4. At first glance, the phase does not appear to be highly non-linear and it would seem that the FFT should be a good match. In fact, as is shown in Section IV, for human targets the phase history is comprised of a linear as well as oscillatory component. Subtracting out the linear component of the phase in Fig. 4, the oscillatory components are revealed (Fig. 5).
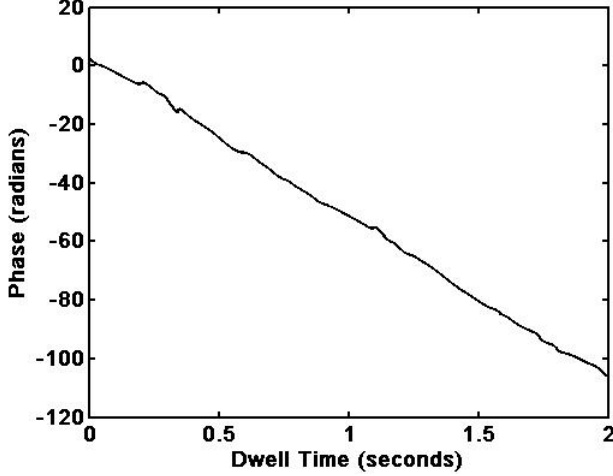

Figure 4. Phase history of a typical human target walking along a vector maximally aligned with the initial antenna-target vector.
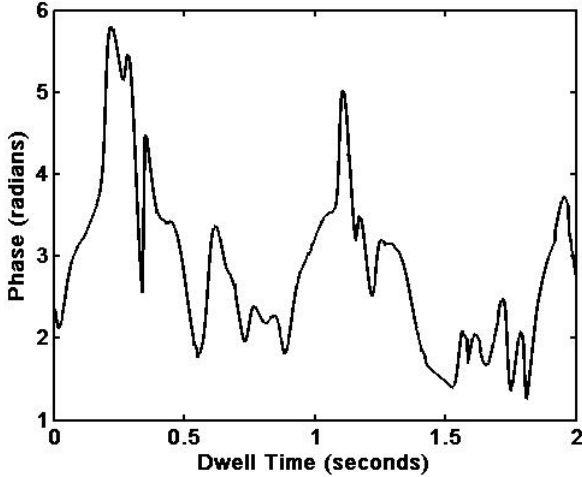

Figure 5. Phase history of Fig. 4 after linear component is removed.

The SNR loss incurred may be quantitatively analyzed as follows. Define the true target data as

$$\mathbf{s} = \begin{bmatrix} \alpha_0 & \alpha_1 e^{j\theta_1} & \cdots & \alpha_{N-1} e^{j(N-1)\theta_{N-1}} \end{bmatrix}^T \qquad (5)$$

where N is the total number of pulses transmitted, and α_i and θ_i are generalized amplitude and phase factors, respectively. Note that in general both the amplitude and phase factors vary with slow-time (n).

When filtered with the weight vector, $w[n]$, the output SNR

is

$$SNR = \frac{E[\mathbf{w}^H \mathbf{s}\mathbf{s}^H \mathbf{w}]}{E[\mathbf{w}^H \mathbf{x_n}\mathbf{x_n}^H \mathbf{w}]} \qquad (6)$$

where x_n is the noise signal. If we assume that the noise has a covariance matrix of $\sigma_n^2 \mathbf{I}$, then (6) may be simplified to

$$SNR = \frac{\left|\mathbf{w}^H \mathbf{s}\right|^2}{\sigma_n^2 \left|\mathbf{w}^H \mathbf{w}\right|} \qquad (7)$$

The maximum output SNR is attained when the received signal s is matched filtered against itself:

$$SNR_0\big|_{\mathbf{w=s}} = \frac{1}{\sigma_N^2} \mathbf{s}^H \mathbf{s} \qquad (8)$$

However, since knowing the target return exactly in advance is impossible, current systems typically matched filter with a linear phase filter, which may be expressed as

$$\mathbf{w_{LIN}} = \begin{bmatrix} \beta_1 & \beta_2 e^{j\phi} & \cdots & \beta_{N-1} e^{j(N-1)\phi} \end{bmatrix}^T, \qquad (9)$$

where β_i and ϕ are generalized amplitude and phase parameters, respectively. Here, the amplitude factor is left in a general form that varies with slow-time, while only the phase has been restricted as linear. The output SNR for such a linear phase filter is

$$SNR_{LIN}\big|_{\mathbf{w=w_{LIN}}} = \frac{\left|\mathbf{w_{LIN}^H s}\right|^2}{\sigma_N^2 \left|\sum_{n=0}^{N-1} \beta_n^2\right|} \qquad (10)$$

Thus, the SNR loss incurred from signal mismatch is

$$SNR\ Loss = \frac{SNR_{LIN}}{SNR_0} = \frac{\left|\mathbf{w_{LIN}^H s}\right|^2}{\left|\sum_{n=0}^{N-1} |\beta_n|^2\right| \mathbf{s}^H \mathbf{s}} \le 1 \qquad (11)$$

There are three main factors which impact SNR loss: phase mismatch, amplitude mismatch, and dwell time. Fig. 6 illustrates the affect of these factors by applying Fourier processing on the example phase history of Fig. 4, which has an amplitude variation of $2.64\times10^{-7}\pm2.5\times10^{-7}$ over a 2 second dwell. The FFT computes a constant, flat-line approximation

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to the true amplitude, i.e. $\beta_n=\beta$ for all n. But the amplitude mismatch – defined as the SNR loss incurred due to amplitude differences, assuming identical phase – is not nearly as significant as the phase mismatch. Over a 2 second dwell, the phase moves through 100 radians, or 5732 degrees, of phase. However, just a 1% error in the slope causes the phase to shift by 2π, an entire cycle. Thus, unlike the amplitude, phase is extremely sensitive to mismatch; despite the gross linear appearance of the phase history, the underlying nonlinearities that are invisible to the naked eye in fact result in SNR losses of up to 30 dB for a 2 second dwell time.
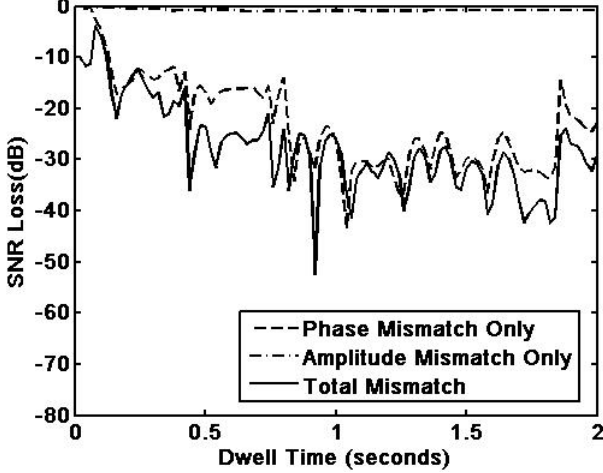

Figure 6. SNR Loss variation over dwell time for the target phase history shown in Fig. 4.

Collecting data over a longer dwell, so that the integration gain increases, also does not help alleviate the inherent SNR loss in Fourier-based, linear phase detectors. Consider the plot in Fig. 7, which shows the trend of the output SNR normalized by input SNR as dwell time is increased for both the ideal, clairvoyant detector and the FFT. While the output SNR continually increases with dwell for the clairvoyant detector, the FFT exhibits on average a flat trend, so that the output SNR does not significantly increase with dwell time. Indeed, the SNR loss, as shown by the difference between the two curves in Fig. 7, simply increases with dwell.

Thus, matched filtering with a more accurate model of the signal phase history has the potential to yield a significant reduction in output SNR losses and, thereby, substantially improve detection performance. For this same example, the model-based optimized nonlinear phase (ONLP) detector proposed in this paper exhibits an SNR loss of only 7 dB for a 2 second dwell time.

The remaining sections of this paper focus on the design and performance of the ONLP detector.
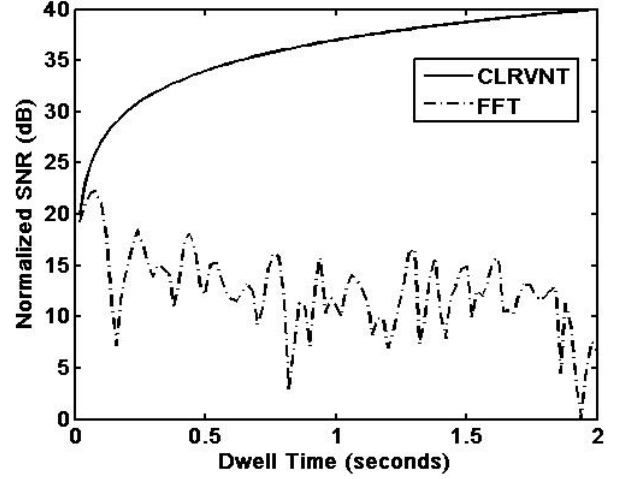

Figure 7. Output SNR variation over dwell time normalized by input SNR for the target phase history shown in Fig. 4 comparing clairvoyant and FFT-based detectors.

IV. DETECTOR DESIGN

A. Detector Formulation

For each range bin centered at r_b, the detector must make a decision between two hypotheses:

$$H_0: \quad \mathbf{x} = \mathbf{x_n}$$
$$H_1: \quad \mathbf{x} = \mathbf{s} + \mathbf{x_n}$$
(12)

where $\mathbf{x_n}$ is complex Gaussian noise with covariance matrix $\mathbf{R_I}$, $\mathbf{s}$ is the true target signal, and we've assumed that there is no range migration, i.e., the entire target return is contained within one range bin. Since the noise covariance matrix cannot be known apriori, an estimate must be used instead. In this paper, we assume clairvoyance:

$$\hat{\mathbf{R}}_{\mathbf{I}} = \mathbf{R_I} = \sigma_n^2 \mathbf{I},$$
(13)

where σ_n^2 is the noise power.

A likelihood ratio test [14, 15] is used to determine the detector decision rule. Under H_0, the noise is distributed as $CN(\mathbf{0}, \hat{\mathbf{R}}_\mathbf{I})$ while under H_1 the noise distribution is $CN(\mathbf{s}, \hat{\mathbf{R}}_\mathbf{I})$, where $\mathbf{s}=\mathbf{x_p}$ is the target signal vector. Thus the decision rule may be expressed as

$$\text{Decide } H_1 \text{ if } \frac{p(\mathbf{x};H_1)}{p(\mathbf{x};H_0)} > \gamma \rightarrow \text{Re}\left\{\mathbf{s^H}\hat{\mathbf{R}}_\mathbf{I}^{-1}\mathbf{x}\right\} > \gamma' \quad (14)$$

where $\gamma' = \sqrt{\text{Re}\{\mathbf{s^H}\hat{\mathbf{R}}_\mathbf{I}^{-1}\mathbf{s}\}} \cdot Q^{-1}(P_{FA})$ and P_{FA} is the desired probability of false alarm.

Since the target return, **s**, is not known apriori, a realizable detector must use an approximation. Our goal in this paper is to develop a better approximation to the target return than that of the linear-phase FFT so as to minimize SNR loss and achieve better detection performance.

The human-model based expression for the target return in (4) is a very good approximation to the true target signal, **s**; however, this model is much too complicated for use as an effective matched filter. The model contains over 24 unknown parameters and most of the kinematic expressions used to compute the time-varying range of each body part are not presented in closed form, but rather as graphs, which must be combined with other charts or equations to derive the time-varying position [9]. Thus, we next derive a simpler, non-linear approximation to (4) that will serve as the basis for our proposed optimized non-linear phase (ONLP) detector.

B. Approximating Expected Target Return

As shown in Fig. 2, the torso response is significantly stronger than the response from the remaining eleven body parts comprising the model, so we will simplify first by neglecting the motion of all body parts except the torso, i.e. we will design the detector to match as best as possible the response from the torso only.

Furthermore, since the overall SNR loss is caused primarily by phase mismatch, we will approximate the received signal amplitude, a_t, as a being constant, A, even though there is some variation across slow-time due to slight variations in gain, RCS, and other loss factors. We also approximate the range term in the amplitude factor (3) with r_b, the center of the range bin at which the peak pulse compression output occurred.

For the range term in the phase, however, we cannot make as crude an approximation, because the phase is much more sensitive to errors than the amplitude. A more accurate approximation to range is obtained as follows.

Define r_1 as the vector from the antenna to the target's initial position and r_N as the vector from the antenna to the target's final position. For simplicity, assume that the human motion is linear along a constant angle, θ, relative to r_1. Then the vector h between the initial and final target locations represents the human motion (Fig. 8).
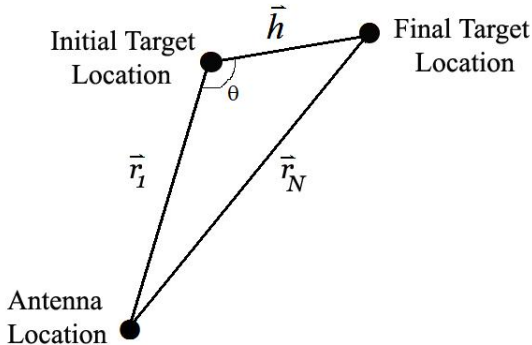

Figure 8. Antenna-target geometry.

Using the law of cosines, we may write

$$|\mathbf{r_n}|^2 = |\mathbf{r_1}|^2 + |\mathbf{h}|^2 - 2|\mathbf{r_1}||\mathbf{h}|\cos\theta. \tag{15}$$

Since $|\mathbf{h}| << |\mathbf{r_1}|$ and $\sqrt{1+x} \approx 1 + x/2$ for small x,

$$|\mathbf{r_n}| \approx |\mathbf{r_1}| - |\mathbf{h}|\cos\theta. \tag{16}$$

Then, (4) may be written as

$$x_p[n] \approx \frac{A}{r_b^2} e^{-j\frac{4\pi f_c}{c}(r - h\cos\theta)}, \tag{17}$$

where r = |$\mathbf{r_1}$| and h = |$\mathbf{h}$|.

The human motion vector h may be more explicitly expressed using the Thalmann kinematic equations as

$$h^2 = OS_V^2 + OS_L^2 + (vTn + OS_{FB})^2, \tag{18}$$

where

$$OS_V = 0.015RV[-1 + \sin(4\pi t\% - 0.7\pi)]$$

$$OS_L = A_L \sin(2\pi t\% - 0.2\pi)$$

$$A_L = \begin{cases} -0.032 & \text{for } 0.5 < RV < 2.3 \\ -0.128RV^2 + 0.128 & \text{for } RV < 0.5 \end{cases}$$

$$OS_{FB} = A_a \sin(4\pi t\% + 2\phi_a)$$

$$A_a = \begin{cases} -0.021 & \text{for } 0.5 < RV < 2.3 \\ -0.084RV^2 + 0.084RV & \text{for } RV < 0.5 \end{cases}$$

$$\phi_a = -0.127 + 0.731\sqrt{RV}$$

Here, OS_L, OS_V, and OS_{FB} represent the lateral, vertical and forward/backward motion of the center of the torso relative to coordinate origin of OS (see Fig. 1) located at the base of the spine. The Thalmann equations depend on only two variables: 1) RV, the ratio of velocity (v) to thigh height (HT); and, 2) t%, a time index taken relative to the beginning of a step. Mathematically, these variables may be expressed as

$$RV = \frac{v}{HT} \tag{19}$$

and

$$t\% = \frac{nT}{1.346}\sqrt{RV} + t_0, \tag{20}$$

where t_0 is a constant indicating the point within the stepping cycle that the first transmitted pulse reflects from the target.

The expression for h may be simplified by throwing out second order terms and approximating the square root as

$$h \approx \sqrt{(vTn)^2 + 2vTnOS_{FB}}$$
$$= vTn\sqrt{1 + \frac{2OS_{FB}}{vTn}} \approx vTn + OS_{FB}. \quad (21)$$

This equation is consistent with the phase histories plotted previously in Fig. 4 and Fig. 5. For small radial velocities, v, the oscillatory term dominates, whereas for large v, the linear term dominates, masking the underlying nonlinearity.

Although generally speaking the phase will contain multiple sinusoids as a result of the quadratic components we previously neglected in (18), too detailed a model will render the detector fragile under noise, so just one sinusoid is used as a nonlinear approximation to the true target phase.

Mathematically, then, the ONLP approximation to the true target phase is

$$x_{onlp}[n] = \frac{A}{r_b^2} e^{j(Mn + C_1 + C_2 \cos(C_3 n + C_4))}, \quad (22)$$

with M, the slope proportional to Doppler frequency; C_1, a factor dependent upon range; C_2, the amplitude of torso motion; C_3, torso frequency; C_4, torso phase; and A, the amplitude as defined in the range equation. These variables are unknown model parameters over which the matched filter response will be optimized.

C. Estimating Model Parameters

The maximum likelihood estimate (MLE) for the any parameter ξ_i in a signal x with mean μ in complex Gaussian noise may be expressed as [16]

$$\frac{\partial \ln(p(\mathbf{x};\xi))}{\partial \xi_i} = 2\mathrm{Re}\left\{ (\mathbf{x} - \mu(\xi))^H \mathbf{C_x^{-1}} \frac{\partial \mu(\xi)}{\partial \xi_i} \right\}. \quad (23)$$

For ξ_i = A,

$$\frac{\partial \mu}{\partial A} = \frac{\partial x_{onlp}}{\partial A} = \frac{1}{r_b^2} e^{j\angle x_{onlp}}. \quad (24)$$

Thus, we set

$$\frac{\partial \ln(p(\mathbf{x};A))}{\partial A} = \frac{2\mathrm{Re}\left\{ \mathbf{x}^H e^{-j\angle \mathbf{x_{onlp}}} - \dfrac{AN}{r_b^2} \right\}}{\sigma^2 r_b^2} = 0, \quad (25)$$

which in turn can be solved to find the MLE:

$$\hat{A} = \frac{r_b^2}{N} \mathrm{Re}\left\{ \mathbf{x}^H e^{-j\angle \mathbf{x_{onlp}}} \right\}$$
$$= \frac{r_b^2}{N} \mathrm{Re}\left\{ \sum_{m=1}^{N} x_m e^{-jx_{onlp,m}} \right\} \quad (26)$$

Although (23) may also be used to estimate the phase parameters, the resulting estimate is not numerically robust. Thus, the MLE for the phase parameters are instead found by first explicitly extracting the phase data. The phase of a complex signal may be found by taking the ratio of the imaginary and real parts. However, this operation also transforms the noise distribution from complex Gaussian to Cauchy, so that the problem may be restated as follows:

$$\tilde{H}_0: \quad \tilde{\mathbf{x}} = \tilde{\mathbf{x}_n}$$
$$\tilde{H}_1: \quad \tilde{\mathbf{x}} = \tan(\angle \mathbf{x_{onlp}}) + \tilde{\mathbf{x}_n} \quad (27)$$

where $\tilde{\mathbf{x}_n}$ is Cauchy distributed noise. Thus, the distribution of $\tilde{\mathbf{x}}$ under H_1 may be computed to be

$$p(\tilde{\mathbf{x}}; \tan(\angle \mathbf{x_{onlp}})) = \frac{1/\pi^N}{\prod_{m=0}^{N-1} \left[1 + \left(\tilde{x}_m - \tan(\angle x_{onlp,m}) \right)^2 \right]}, \quad (28)$$

where $\tilde{x}_m \equiv [\tilde{\mathbf{x}}]_m$, the mth element of $\tilde{\mathbf{x}}$.

The MLE for an unknown parameter ξ_i is given by solving the following equation for each ξ_i:

$$\frac{\partial}{\partial \xi_i} \ln p(\tilde{\mathbf{x}}; \tan(\angle \mathbf{x_{onlp}}), \gamma) = 0, \quad (29)$$

which can be reduced to

$$\sum_{m=0}^{N-1} \frac{\tilde{x}_m - \tan(\angle x_{onlp,m})}{1 + \left(\tilde{x}_m - \tan(\angle x_{onlp,m}) \right)^2} \frac{\partial}{\partial \xi_i} \tan(\angle x_{onlp,m}) = 0 \quad (30)$$

Computing of the MLE estimates for all 5 phase parameters thus requires solving a system of 5 nonlinear equations, which is impossible to do in closed form, and very computationally and memory intensive even when solved numerically.

Therefore, we break the problem into two stages by first estimating the linear component, and then estimating the non-linear term.

If in (17) we model the human motion as being simply that of a constant-velocity point target, then $h = nvT$ and

$$x_p[n] \approx \frac{A}{r_b^2} e^{-j\frac{4\pi f_c}{c}(r - nTv_r)}, \qquad (31)$$

where $v_r = v\cos\theta$. The two unknown linear phase parameters r and v_r may then be found by solving the least squares problem $\mathbf{A}\boldsymbol{\xi} = \mathbf{b}$ as

$$\hat{\boldsymbol{\xi}} = \left(\mathbf{A}^T\mathbf{A}\right)^{-1}\mathbf{A}^T\mathbf{b}, \qquad (32)$$

where

$$\mathbf{A} = \frac{4\pi f_c}{c}\begin{bmatrix} T & 2T & \cdots & NT \\ -1 & -1 & \cdots & -1 \end{bmatrix}^T$$

$$\hat{\boldsymbol{\xi}} = \begin{bmatrix} r & v_r \end{bmatrix}^T$$

$$\mathbf{b} = \begin{bmatrix} \tan^{-1}(\tilde{x}_1) & \tan^{-1}(\tilde{x}_2) & \cdots & \tan^{-1}(\tilde{x}_N) \end{bmatrix}^T$$

An initial estimate of the slope M may then be found as

$$M_i = \frac{4\pi f_c}{c}Tv_r = \frac{4\pi f_c}{c}T\hat{\xi}(2) \qquad (33)$$

This initial estimate is then numerically refined so as to ensure no residual linear component remains.

Having computed an estimate for the slope M, the remaining parameters in the nonlinear component of the phase are estimated from (30), which is now reduced to a system of four nonlinear equations and four unknowns, solved using numerical iteration. Note that of these four parameters, the frequency and phase shift coefficients C_3 and C_4 are the most crucial for ensuring the best match between model and data. Thus, to save computation time, larger step sizes are used for C_1 and C_2, while finer step sizes are utilized for C_3 and C_4.

The final form of our proposed ONLP detector is

$$\text{Re}\left\{\hat{\mathbf{x}}_{\mathbf{onlp}}^{\mathbf{H}}\hat{\mathbf{R}}_{\mathbf{I}}^{-1}\mathbf{x}\right\} > \gamma' \qquad (34)$$

where $\gamma' = \sqrt{\text{Re}\{\hat{\mathbf{x}}_{\mathbf{onlp}}^{\mathbf{H}}\hat{\mathbf{R}}_{\mathbf{I}}^{-1}\hat{\mathbf{x}}_{\mathbf{onlp}}\}} \cdot Q^{-1}(P_{FA})$, which is still a linear detector as the elements of x_{onlp} merely form the weights with which we filter our signal.

D. Quality of Parameter Estimates

Obtaining adequate estimates of the unknown model parameters is critical to the performance of the matched filter detector. The estimation problem, however, is affected by several factors, including the direction of motion (i.e. target geometry), dwell time, and SNR.

As indicated by (21), the phase history of a human target may be represented as the sum of linear and oscillatory components. Depending on the target geometry and walking speed, the shape of the phase history may vary. When the target moves roughly perpendicular to the antenna-target vector, the radial velocity will be nearly zero and the

oscillatory component is clearly apparent. As the target moves along the antenna-target vector, the radial velocity is almost identical to the true target velocity, so the linear component has more of an affect.

The dwell time is also an important factor, as the amount of data collected limits the number of cycles we can observe. For example, at extremely short dwells, the phase history may only have a mild nonlinearity, similar to a bowed curve or a quarter-cycle of a sinusoid. Finally, SNR is also a critical factor, since as the noise level increases the true signal curvature is obscured, leading to degradation in our parameter estimates. For low SNRs, longer dwell times will be required for good parameter estimates.

The quality of the parameter estimates may be assessed using the Cramer-Rao Bound (CRB). It can be shown that for a general signal $x[n, \boldsymbol{\theta}]$ in complex Gaussian noise with variance σ^2, the CRB is given by [16]

$$\text{var}(\hat{\theta}) \geq \frac{1}{I(\theta)|_{ij}} = \left[\frac{2}{\sigma^2}\text{Re}\left\{\sum_{n=0}^{N-1}\frac{\partial x^H}{\partial\theta_i}\frac{\partial x}{\partial\theta_j}\right\}\right]^{-1}, \quad (35)$$

where $I(\boldsymbol{\theta})$ is the Fisher information matrix. Evaluating (34) for the expression of x_{onlp} given in (22), the desired CRB may be analytically expressed as

$$\text{var}(\hat{\boldsymbol{\theta}}) \geq diag\left\{\frac{1}{4 \cdot SNR}\mathbf{B}^{-1}(\hat{\boldsymbol{\theta}})\right\} \qquad (36)$$

where the pulse-wise SNR is defined as $A^2/2r_b^2\sigma^2$ and

$$B(\theta) = \begin{bmatrix} N & S_1 & C_2S_2 & C_2S_3 & 0 \\ S_1 & S_4 & C_2S_5 & C_2S_6 & 0 \\ C_2S_2 & C_2S_5 & C_2^2S_7 & C_2^2S_8 & 0 \\ C_2S_3 & C_2S_6 & C_2^2S_8 & C_2^2S_9 & 0 \\ 0 & 0 & 0 & 0 & \frac{N}{A^2} \end{bmatrix}$$

$$S_1 \equiv \sum_{n=0}^{N-1}\cos(C_3n + C_4); \quad S_2 \equiv \sum_{n=0}^{N-1}n\sin(C_3n + C_4)$$

$$S_3 \equiv \sum_{n=0}^{N-1}\sin(C_3n + C_4); \quad S_4 \equiv \sum_{n=0}^{N-1}\cos^2(C_3n + C_4);$$

$$S_5 \equiv \sum_{n=0}^{N-1}n\sin(C_3n + C_4)\cos(C_3n + C_4);$$

$$S_6 \equiv \sum_{n=0}^{N-1}\sin(C_3n + C_4)\cos(C_3n + C_4);$$

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$$S_7 \equiv \sum_{n=0}^{N-1} n^2 \sin^2\left(C_3 n + C_4\right); \quad S_8 \equiv \sum_{n=0}^{N-1} n \sin^2\left(C_3 n + C_4\right);$$

$$S_9 \equiv \sum_{n=0}^{N-1} \sin^2\left(C_3 n + C_4\right).$$

In Fig. 9, the CRB on $\hat{C}_1$ is plotted together with the simulated variance of $\hat{C}_1$ under two cases: 1) The underlying data is exactly the same as the model $\mathbf{x}_{ONLP}$ in (22) used to compute the CRB; and, 2) the underlying data is the synthetic human data representative of true human motion as given in (4). The MLE estimator achieves the performance of the
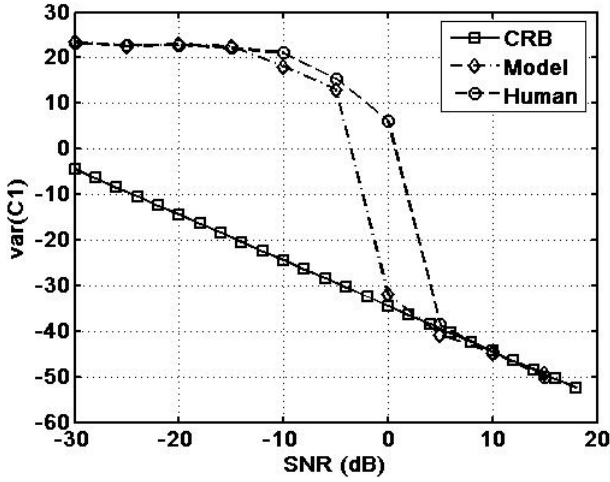

Figure 10. Variation of linear phase parameter, M, MLE versus number of pulses transmitted over 100 Monte Carlo trials.

Figure 9. CRB and variance of parameter (C_1) MLE with ONLP approximation over 500 Monte Carlo trials.

CRB for single-pulse SNRs above 5 dB. Notice that for intermediate SNR values, there is a slight difference between the simulated variances when the model data and synthetic human data are used. For example, when the underlying data exactly matches the model, the estimates follow the CRB for SNRs above 0 dB. This 5 dB difference illustrates the impact of modeling error on the estimates. However, the fact that the variances match for most SNRs also validates the quality of the ONLP model in terms of approximating the true data.

The dwell time – i.e., the number of pulses transmitted during the entire data collect times the PRI – also has a significant impact on the quality of the parameter estimates. As illustrated in Fig. 10, the longer the dwell time, the better the estimate. Thus, when the SNR is very low, as is typical of human targets, data must be collected for a much longer time to achieve comparable performance to targets with a higher SNR (or RCS).

In this case, the estimate for the linear phase parameter, M, stabilizes after a 1.5 second dwell time when the SNR is 20 dB; but when the SNR is -20 dB, the estimate stabilizes after 2.4 seconds. In other words, for this particular example, to achieve the same quality of estimate, an additional 0.9 seconds of data must be collected.
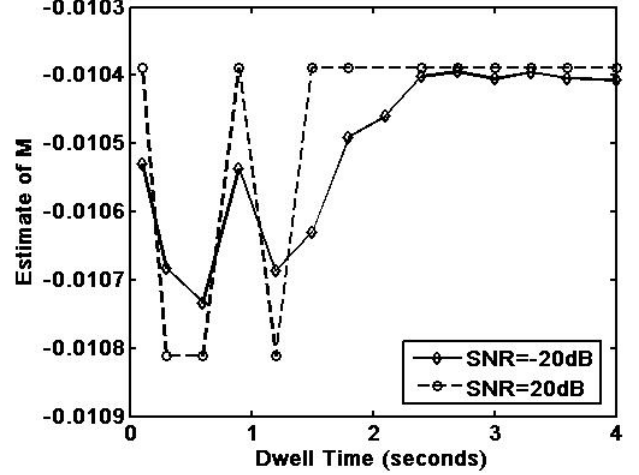
V. PERFORMANCE

Detector performance is evaluated by applying the proposed ONLP detector to simulated radar data as generated in (4). The receiver operating characteristic (ROC) curves as well as the impact of SNR, incidence angle, and dwell time on the probability of detection (P_D) is assessed. By incidence angle, we mean the angle between the initial antenna-target vector and the target motion vector. Additionally, the effect on detection performance of multiple human targets within a single range bin is analyzed. The results presented in Fig. 11 – Fig. 15 are generated for a radar with the characteristics shown in Table 1.

TABLE 1

Center Frequency	1 GHz
Sampling Frequency	20 MHz
Bandwidth	10 MHz
Pulse Repetition Interval	0.2 ms
Pulse Width	40 µs
Transmit Power	1.8 kW
Nominal Range	8,760 m

A. Receiver Operating Characteristics

ROC curves for the clairvoyant, FFT, and ONLP detectors are shown for a human target walking parallel to the x-axis and with an incidence angle of 135° in Fig. 11. The proposed ONLP detector exhibits similar performance to the ideal clairvoyant detector at a PFA of 0.5, whereas the FFT never approaches ideal performance until the PFA is about 1. The ONLP performance exceeds that of the FFT for all PFAs.
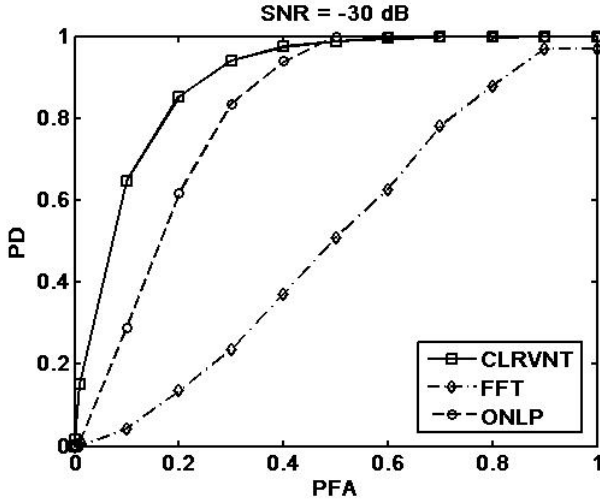
9

Figure 11. P_D vs. P_{FA} for a human target with an incidence angle of 135°, a dwell time of 0.5 s. and single-pulse SNR = -30dB.

B. *Probability of Detection Versus SNR*

The performance improvement of the proposed technique may also be seen in Fig. 12, which shows the affect of SNR on the probability of detection. The ONLP detector yields about an 11dB improvement in output SNR relative to the FFT.
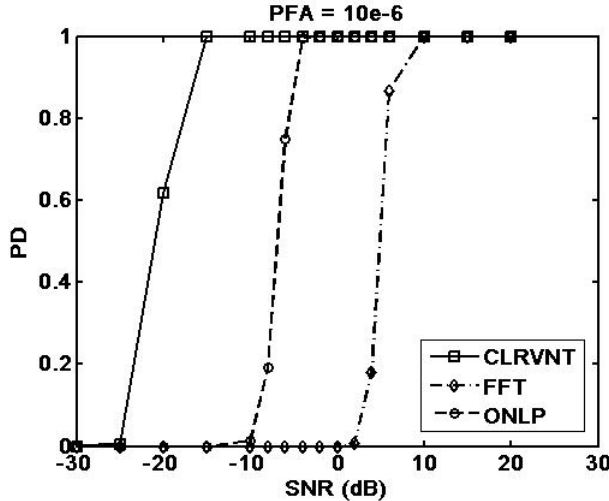

Figure 12. P_D vs. SNR for a human target with an incidence angle of 135°, a dwell time of 0.5 s. and P_{FA}=10⁻⁶.

C. *Impact of Target Motion on Detection*

The ONLP method maintains this performance gain regardless of the target direction of motion. Fig. 13 shows the probability of detection variation over incidence angle for both the FFT and ONLP methods. Note that performance of the FFT plummets as that target's motion increasingly aligns with the radar-target vector. This is because as the radial velocity observed by the radar increases, the overall phase history becomes increasingly linear. Even a small error in estimating the phase history slope results in errors that accrue with dwell time and severely degrade performance. When the radial

velocity is small, the phase history is predominantly sinusoidal and the phase mismatch errors are limited by the oscillation amplitude. Because the ONLP method optimizes the matched filter parameters, it maintains superior performance over all incidence angles.
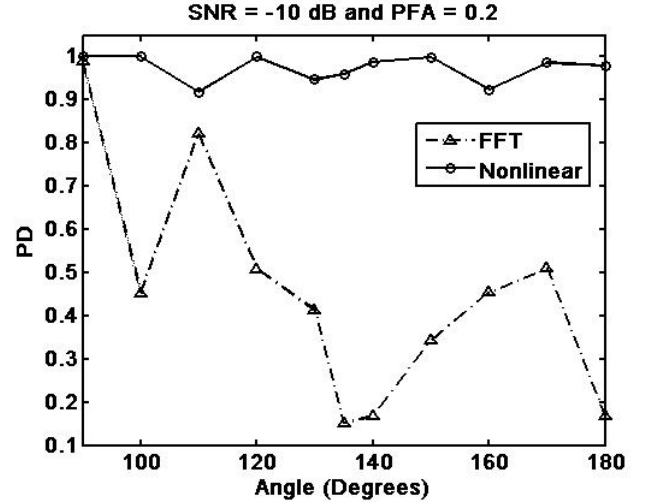

Figure 13. P_D vs. incidence angle for a human target with a dwell time of 0.5 s., SNR of -10dB and P_{FA}=0.2.

D. *Probability of Detection Versus Dwell Time*

The impact of dwell time on detection performance is shown in Fig. 14. After a dwell of about 1.2 seconds, the proposed ONLP detector achieves the same performance as the ideal, clairvoyant detector. However, the FFT-based detector is unable to detect any targets even after twice the dwell time. This result is consistent with expectations, as the output SNR versus dwell time plot of Fig. 7 also showed that for human detection FFT-based detectors do not exhibit improved performance with dwell time. By making a significantly better matched filter, however, not only are we able to achieve better detection performance at a given dwell time, but we are now able to eventually achieve ideal performance given a sufficiently long dwell.

E. *Multi-Target Situation*

Up until now, results have been provided for the case when a single target resides in a single range bin. However, considering human social patterns, more than one human target occupying the same range-bin is very likely, causing the phase history to, in fact, contain the sum of the phase information of multiple human targets. In this situation, we define a detection as the simple indication of a target present, not the determination of the number of targets present, a topic of future work.

Consider the case of three people starting at the same point, but walking in different directions: 45°, 0°, and -45° relative to x-axis. Then, the phase history obtained for a total number of 2,500 transmitted pulses consists of irregularly shaped oscillations, as shown in Fig. 15.
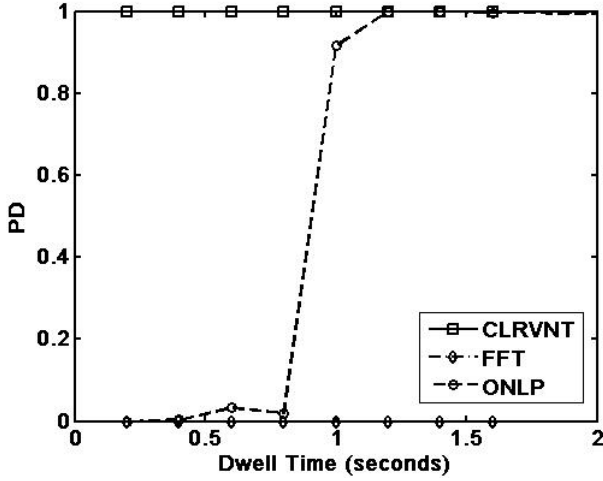
10

Figure 14. P_D v dwell time for a human target with an SNR of -10dB and $P_{FA}=10^{-6}$.
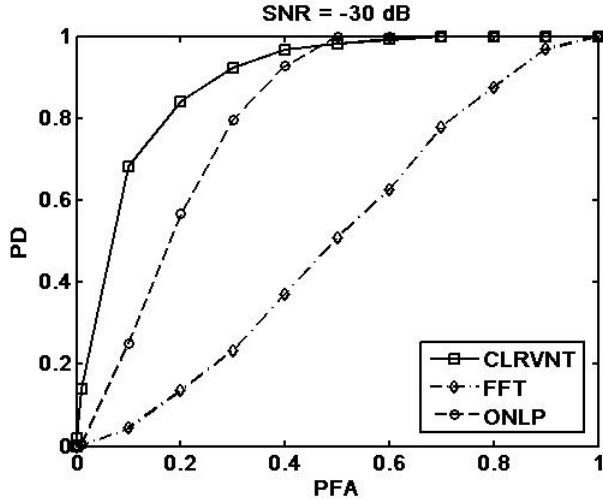

Figure 16. ROC curve comparing detector performance for the multi-target phase history of Fig. 15.

thereby capturing the characteristic nature of human motion. Results show a drastic improvement in output SNR and detection performance for the proposed method relative to existing FFT-based techniques.
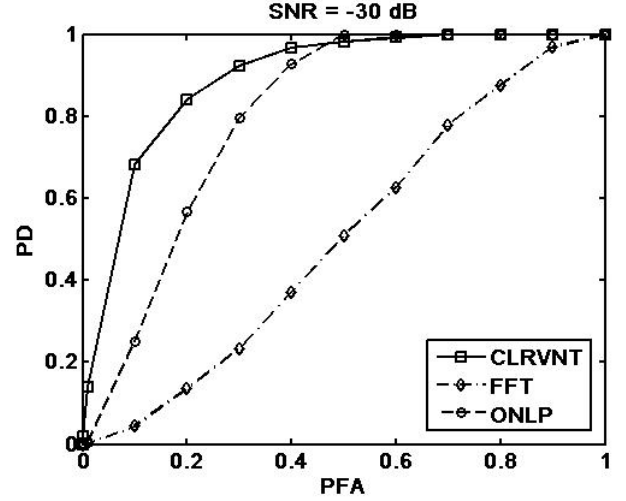

Figure 16. ROC curve comparing detector performance for the multi-target phase history of Fig. 15.

Possibilities for future work include extending this technique to multi-channel systems so that clutter cancellation techniques may be used to mitigate the effect of clutter; applying spectral analysis techniques to estimate the number of human targets detected within a range bin; and using the Thalmann model to extract additional information about the target. For example, an estimate of the velocity/height ratio, RV, may be obtained and used, in conjunction with the velocity estimate, to extract an estimate of the person's height. Statistical properties of the variation of human height in men and women may then be used to classify targets according to gender.

These irregularities do not significantly affect the detector design, as any nonlinearity is matched filtered with the best-fitting sinusoid, and thereby achieves improved detection performance, as shown in Fig. 16. Generally, the higher the number of targets in a range bin, the more complex and nonlinear the phase function. Although in an absolute sense, the degree to which the model matches the phase in the multi-target case may vary, the ONLP model will almost always better match the phase of – and thus outperform – the linear phase FFT.

VI. CONCLUSION

A novel method for improving the performance of matched-filters in detecting human targets has been presented. A sinusoidal (ONLP) approximation to the true target phase was derived based on the Thalmann human walking model,

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